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17MAT31

## Third Semester B.E. Degree Examination, Aug./Sept. 2020 Engineering Mathematics – III

Time: 3 hrs.

Max. Marks: 100

**Note: Answer any FIVE full questions, choosing ONE full question from each module.**

### Module-1

- 1 a. Find the Fourier series to represent the periodic function  $f(x) = x - x^2$  from  $x = -\pi$  to  $x = \pi$ . (08 Marks)
- b. The following table gives the variations of periodic current over a period.

t sec	0	$\frac{T}{6}$	$\frac{T}{3}$	$\frac{T}{2}$	$\frac{2T}{3}$	$\frac{5T}{6}$	T
A amp.	1.98	1.30	1.05	1.30	-0.88	-0.25	1.98

Expand A as a Fourier series upto first harmonic. Obtain the amplitude of the first harmonic. (06 Marks)

- c. Find the half range cosine series for the function  $f(x) = (x - 1)^2$  in  $0 < x < 1$ . (06 Marks)

**OR**

- 2 a. Find the Fourier series of  $f(x) = 2x - x^2$  in  $(0, 3)$ . (08 Marks)
- b. Obtain the constant term and the coefficients of the first sine and cosine terms in the Fourier series expansion of y as given in the following table: (06 Marks)

x:	0	1	2	3	4	5	6
y:	9	18	24	28	26	20	9

- c. Obtain the half-range sine series for the function,

$$f(x) = \begin{cases} x, & 0 < x < \frac{\pi}{2} \\ \pi - x, & \frac{\pi}{2} < x < \pi \end{cases} \quad (06 \text{ Marks})$$

### Module-2

- 3 a. Find the Fourier transform of  $f(x) = \begin{cases} a^2 - x^2, & |x| \leq a \\ 0, & |x| > a \end{cases}$ . Hence deduce that

$$\int_0^{\infty} \frac{(\sin x - x \cos x)}{x^3} \cos \frac{x}{2} dx = \frac{3\pi}{16} \quad (08 \text{ Marks})$$

- b. Find the Z-transform of,  
(i)  $\cos n\theta$  and (ii)  $\cosh n\theta$  (06 Marks)
- c. Solve  $y_{n+2} + 6y_{n+1} + 9y_n = 2^n$  with  $y_0 = 0 = y_1$ , using z-transforms technique. (06 Marks)



OR

- 4 a. Find the Fourier cosine transform of  $e^{-ax}$ . Hence evaluate  $\int_0^{\infty} \frac{\cos \lambda x}{x^2 + a^2} dx$  (08 Marks)
- b. Find the Z-transform of,  
(i)  $(n+1)^2$  (ii)  $\sin(3n+5)$  (06 Marks)
- c. Find the inverse Z-transform of  $\frac{2z^2 + 3z}{(z+2)(z-4)}$ . (06 Marks)

**Module-3**

- 5 a. Find the two regression lines and hence the correlation coefficient between x and y from the data. (08 Marks)

x	1	2	3	4	5	6	7	8	9	10
y	10	12	16	28	28	36	41	49	40	50

- b. Fit a second degree parabola to the following data: (06 Marks)

x	0	1	2	3	4
y	1	1.8	1.3	2.5	6.3

- c. Using Newton-Raphson method find the root of  $x \sin x + \cos x = 0$  near  $x = \pi$  corrected to 4 decimal places. (06 Marks)

OR

- 6 a. Two variables x and y have the regression lines  $3x + 2y = 26$  and  $6x + y = 31$ . Find the mean values of x and y and the correlation coefficient between them. (08 Marks)

- b. Fit a curve of the form,  $y = ae^{bx}$  to the following data: (06 Marks)

x:	5	15	20	30	35	40
y:	10	14	25	40	50	62

- c. Using Regula-Falsi method find the root of  $xe^x = \cos x$  in the interval (0, 1) carrying out four iterations. (06 Marks)

**Module-4**

- 7 a. Using Newton's forward and backward interpolation formulae, find  $f(1)$  and  $f(10)$  from the following table: (08 Marks)

x	3	4	5	6	7	8	9
f(x)	4.8	8.4	14.5	23.6	36.2	52.8	73.9

- b. Given that  $f(5) = 150$ ,  $f(7) = 392$ ,  $f(11) = 1452$ ,  $f(13) = 2366$ ,  $f(17) = 5202$ . Using Newton's divided difference formulae find  $f(9)$ . (06 Marks)

- c. Using Simpson's  $\frac{1}{3}$  rule evaluate  $\int_0^{0.6} e^{-x^2} dx$  by taking seven ordinates. (06 Marks)

OR

- 8 a. Using Newton's Backward difference interpolation formula find  $f(105)$  from, (08 Marks)

x	80	85	90	95	100
f(x)	5026	5674	6362	7088	7854

- b. If  $f(1) = -3$ ,  $f(3) = 9$ ,  $f(4) = 30$ ,  $f(6) = 132$  find Lagrange's interpolation polynomial that takes the same value as  $f(x)$  at the given point. (06 Marks)

- c. Evaluate  $\int_4^{5.2} \log_e x dx$  by Simpson's  $\frac{3}{8}$  rule with  $h = 0.1$ . (06 Marks)

**Module-5**

- 9 a. Verify Green's theorem for  $\oint_C (xy + y^2)dx + x^2dy$  where C is bounded by  $y = x$  and  $y = x^2$ .

(08 Marks)

- b. Using Gauss divergence theorem evaluate  $\iiint_S \vec{F} \cdot \hat{n} ds$ ,

where  $\vec{F} = (x^2 - yz)\hat{i} + (y^2 - zx)\hat{j} + (z^2 - xy)\hat{k}$  over the rectangular parallel piped  $0 \leq x \leq a$ ,  $0 \leq y \leq b$  and  $0 \leq z \leq c$ .

(06 Marks)

- c. With usual notations derive Euler's equation,  $\frac{\partial f}{\partial y} - \frac{d}{dx} \left( \frac{\partial f}{\partial y'} \right) = 0$ .

(06 Marks)

**OR**

- 10 a. If  $\vec{F} = (5xy - 6x^2)\hat{i} + (2y - 4x)\hat{j}$ , evaluate  $\oint_C \vec{F} \cdot d\vec{r}$  along the curve C in the xy-plane,  $y = x^3$  from (1, 1) to (2, 8).

(08 Marks)

- b. Find the extremals of the functional with  $y(0) = 0$  and  $y(1) = 1$ .

(06 Marks)

- c. Show that Geodesics on a plane arc straight lines.

(06 Marks)

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